

# Broadcast Steganography or How to Broadcast a Secret *Covertly*

SESSION ID: CRYPT-08

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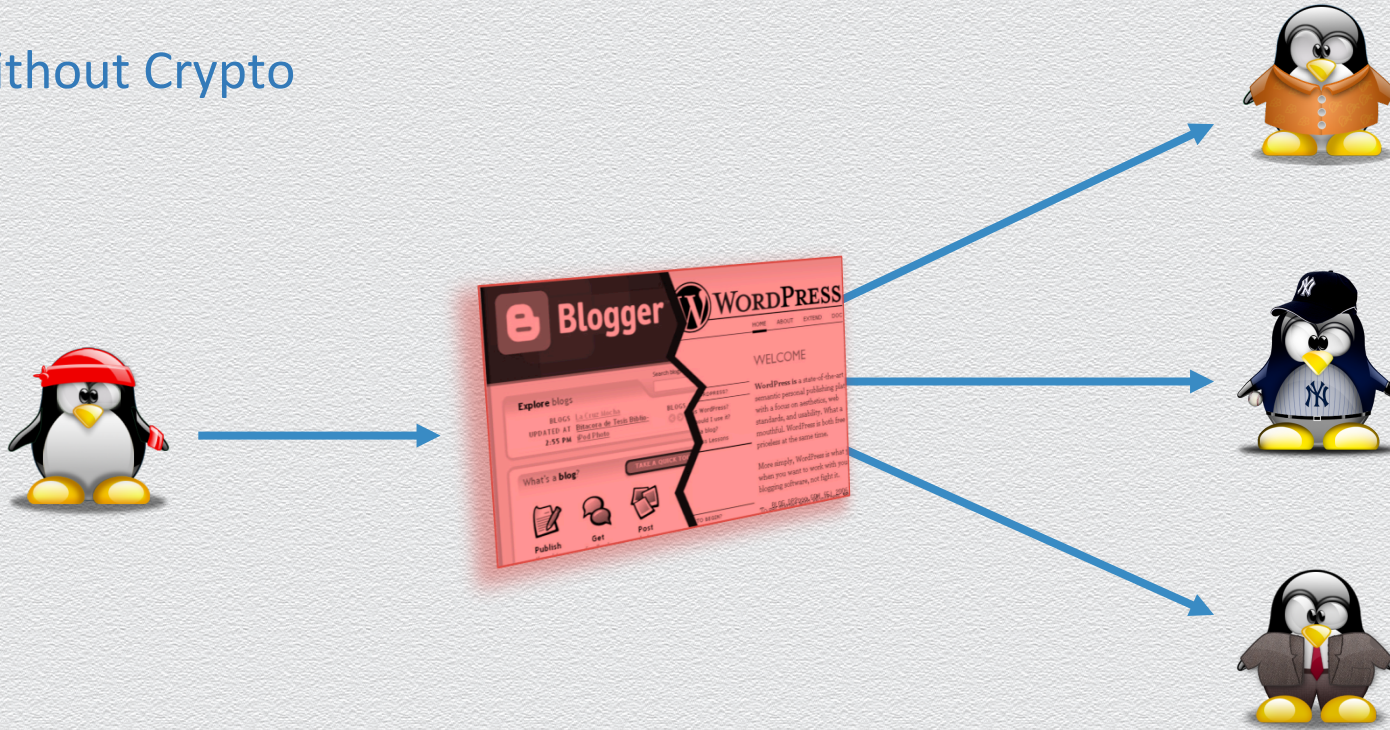


# Without Crypto



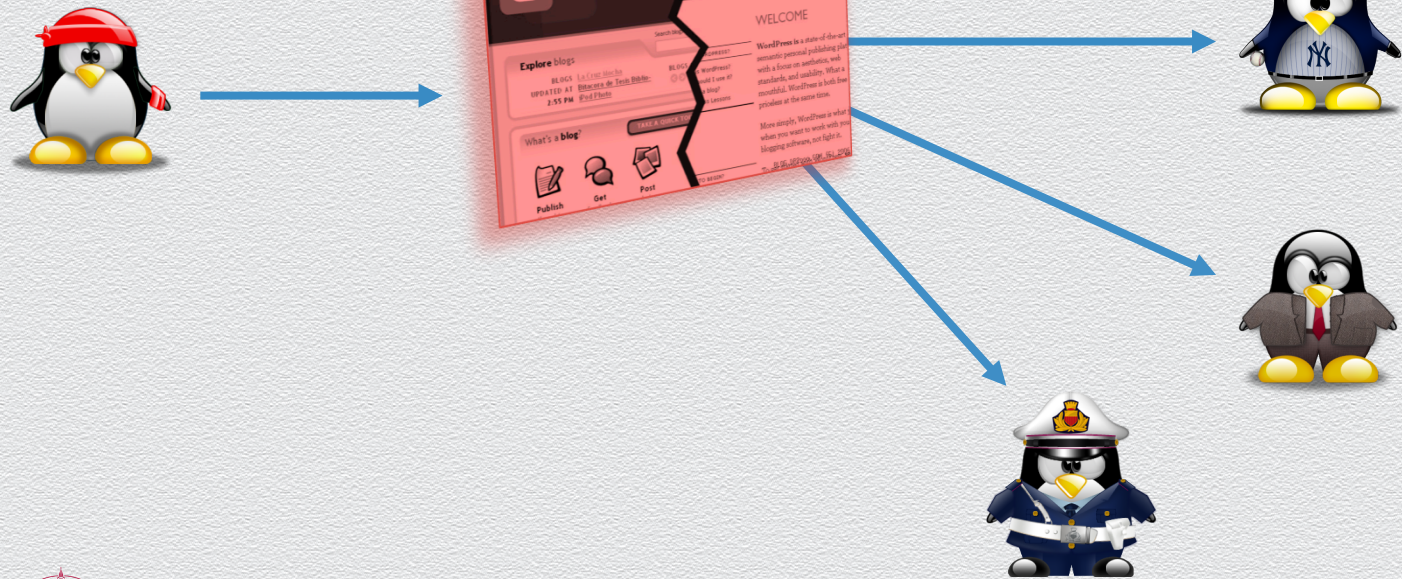


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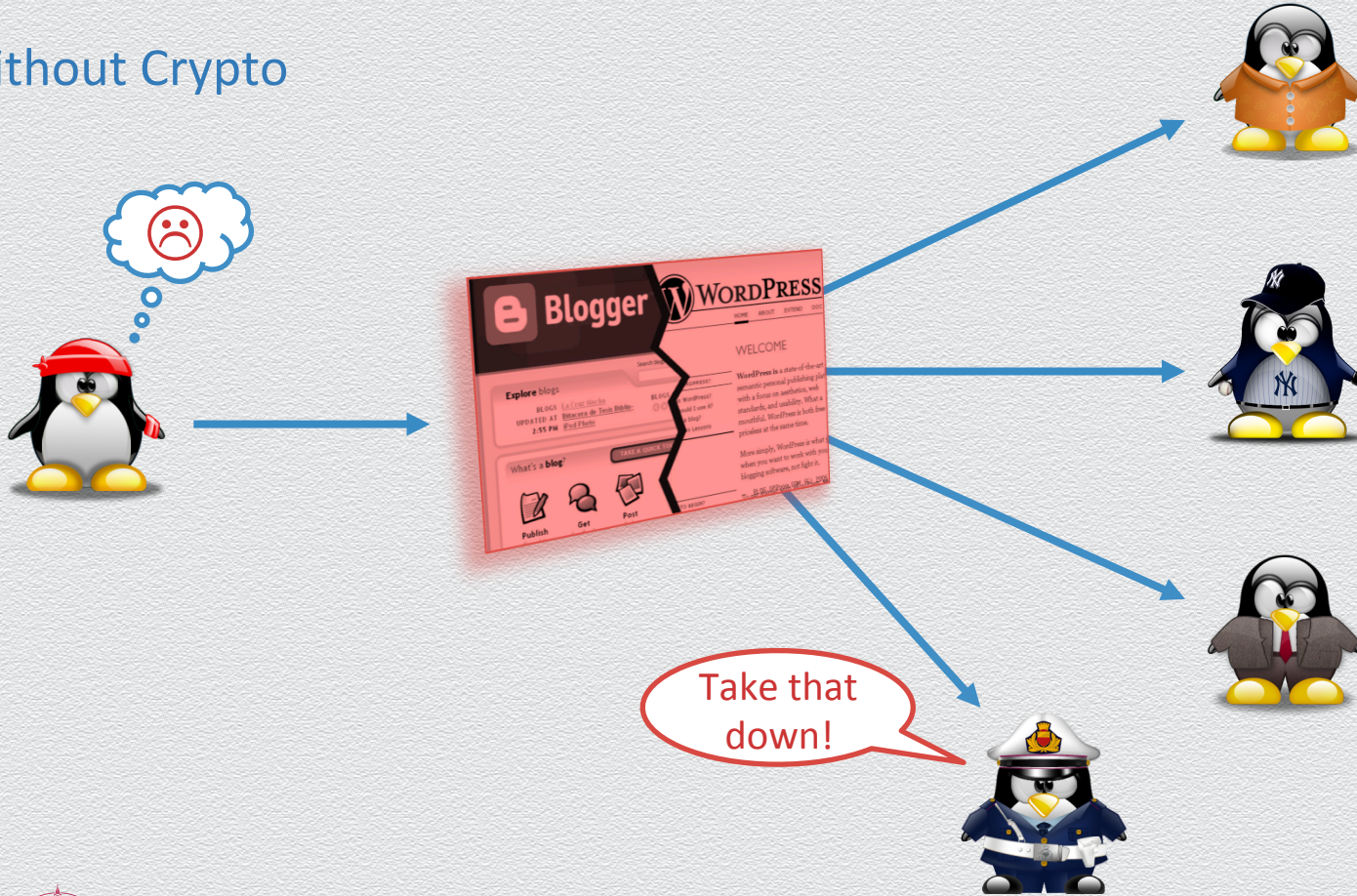


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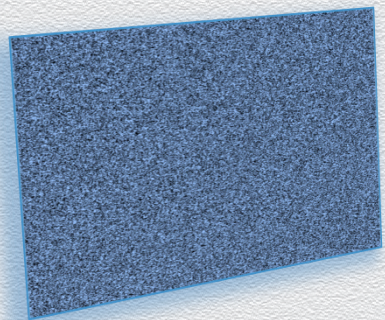


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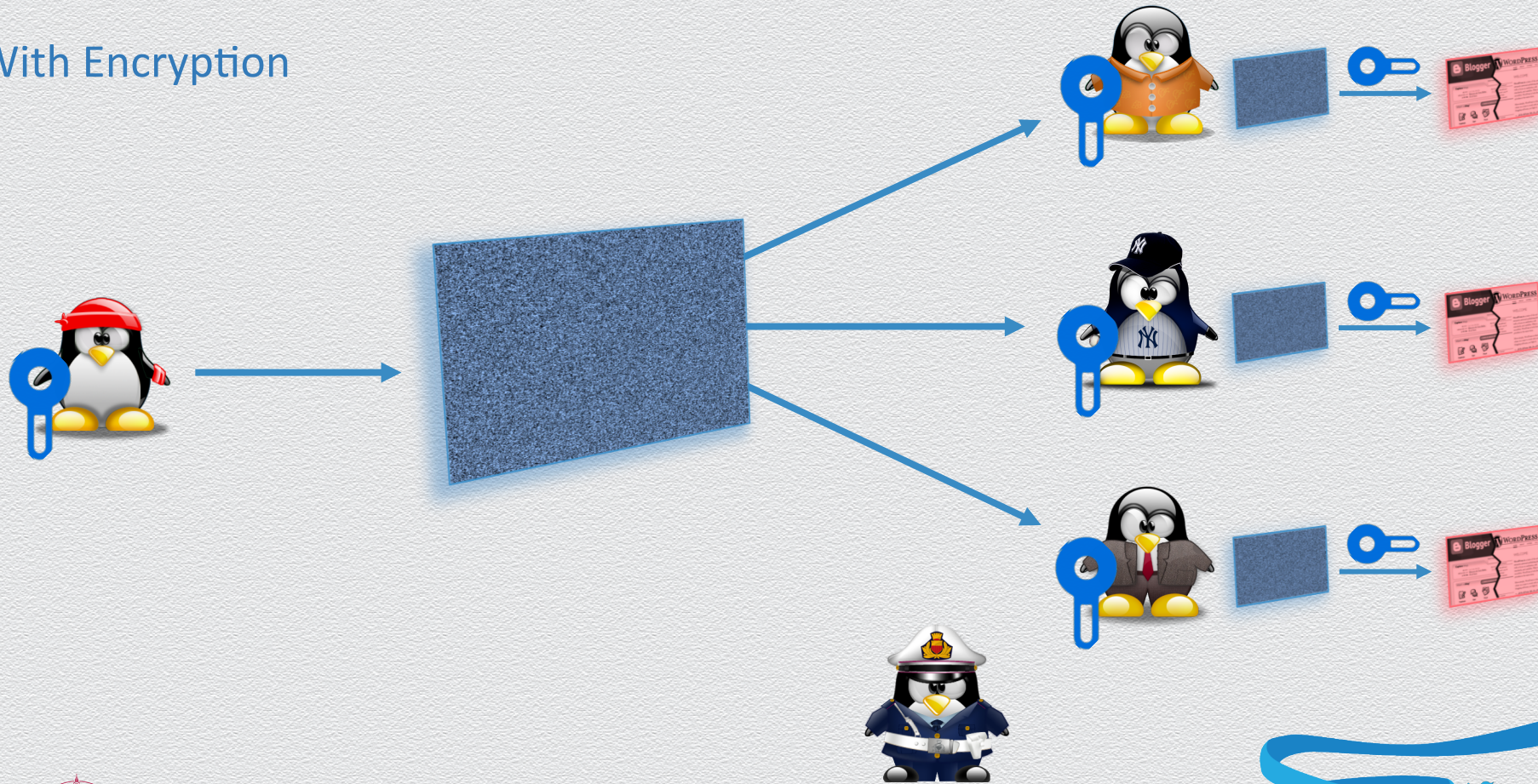


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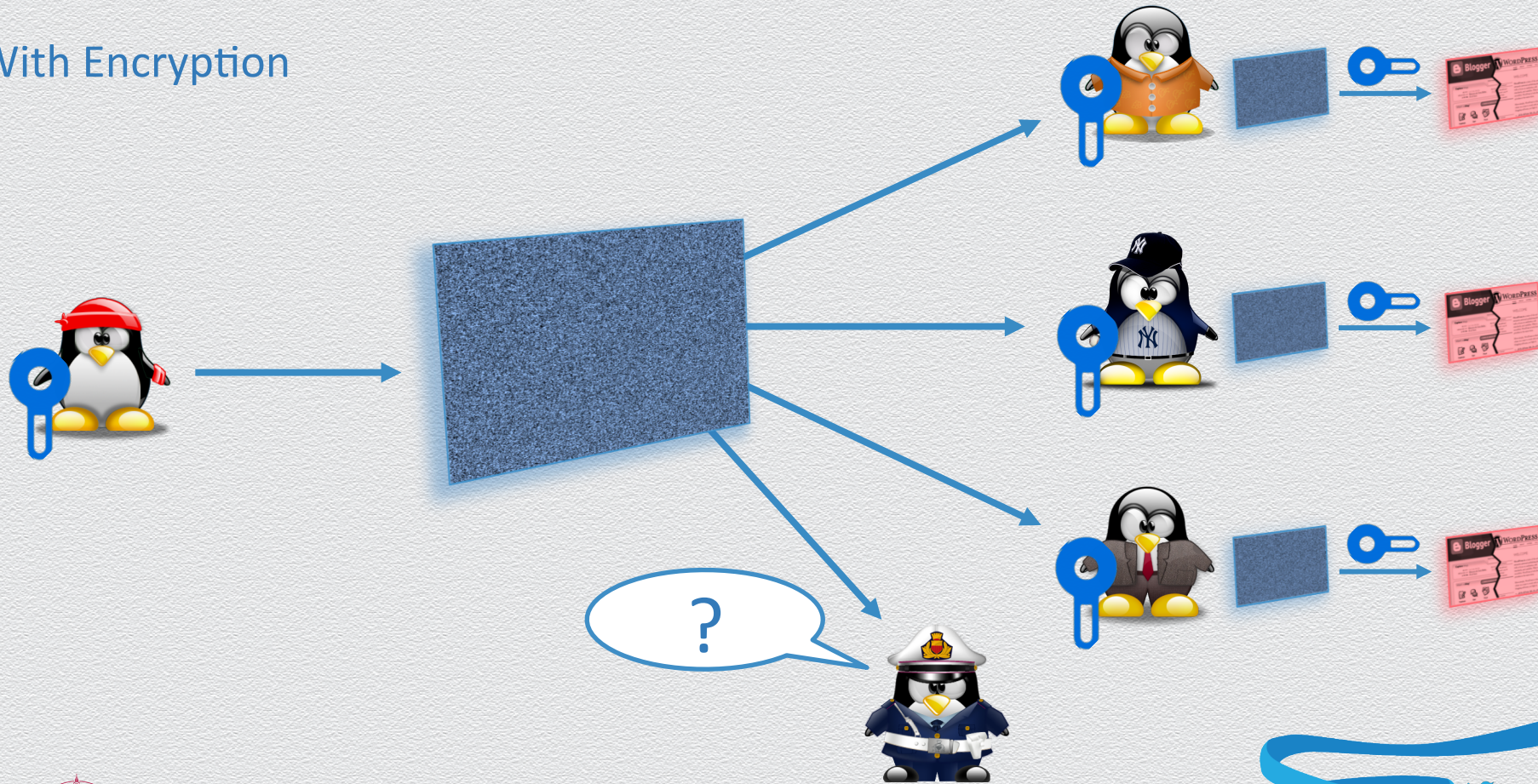


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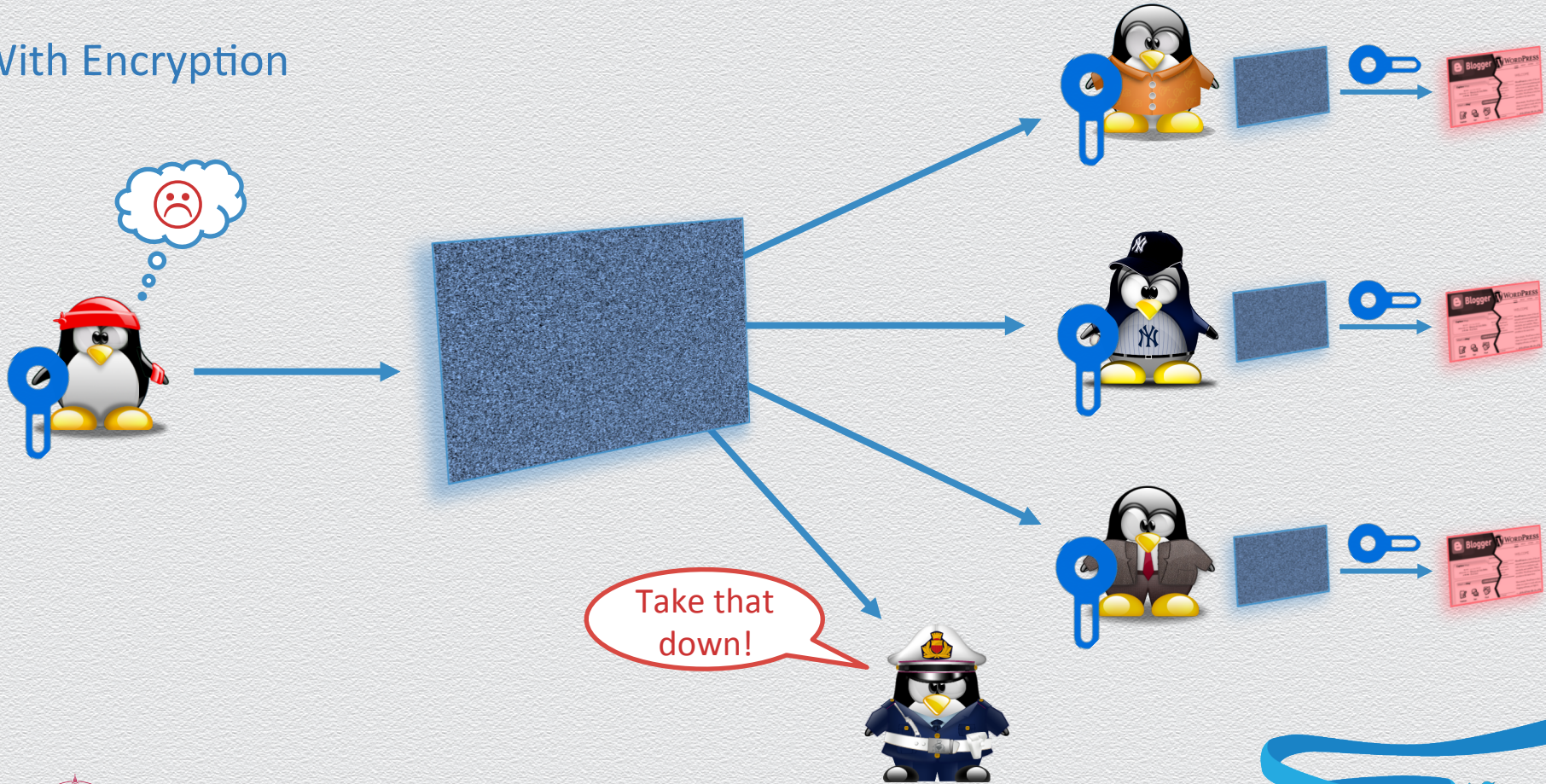


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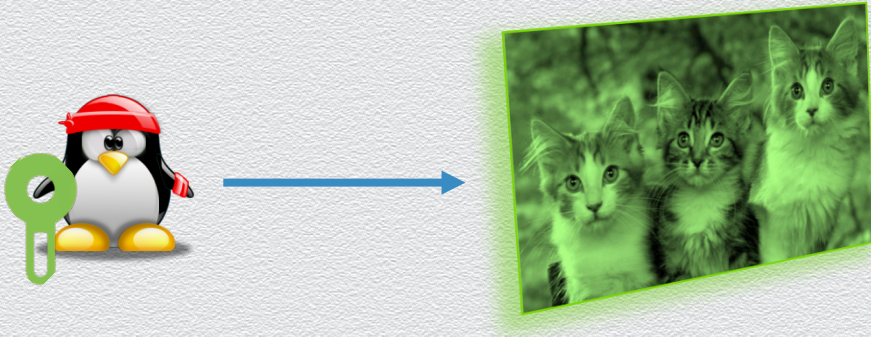


# With Steganography



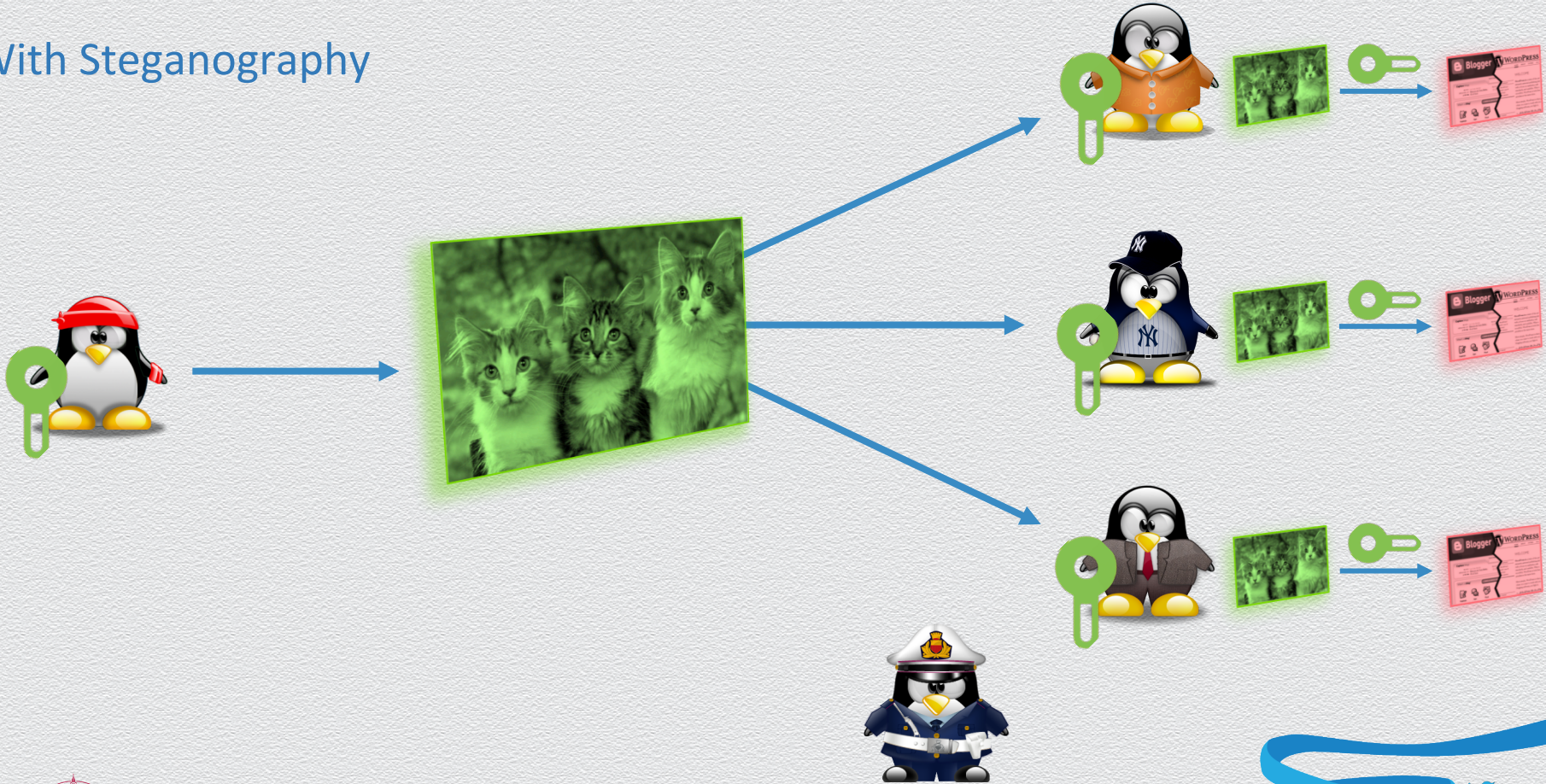


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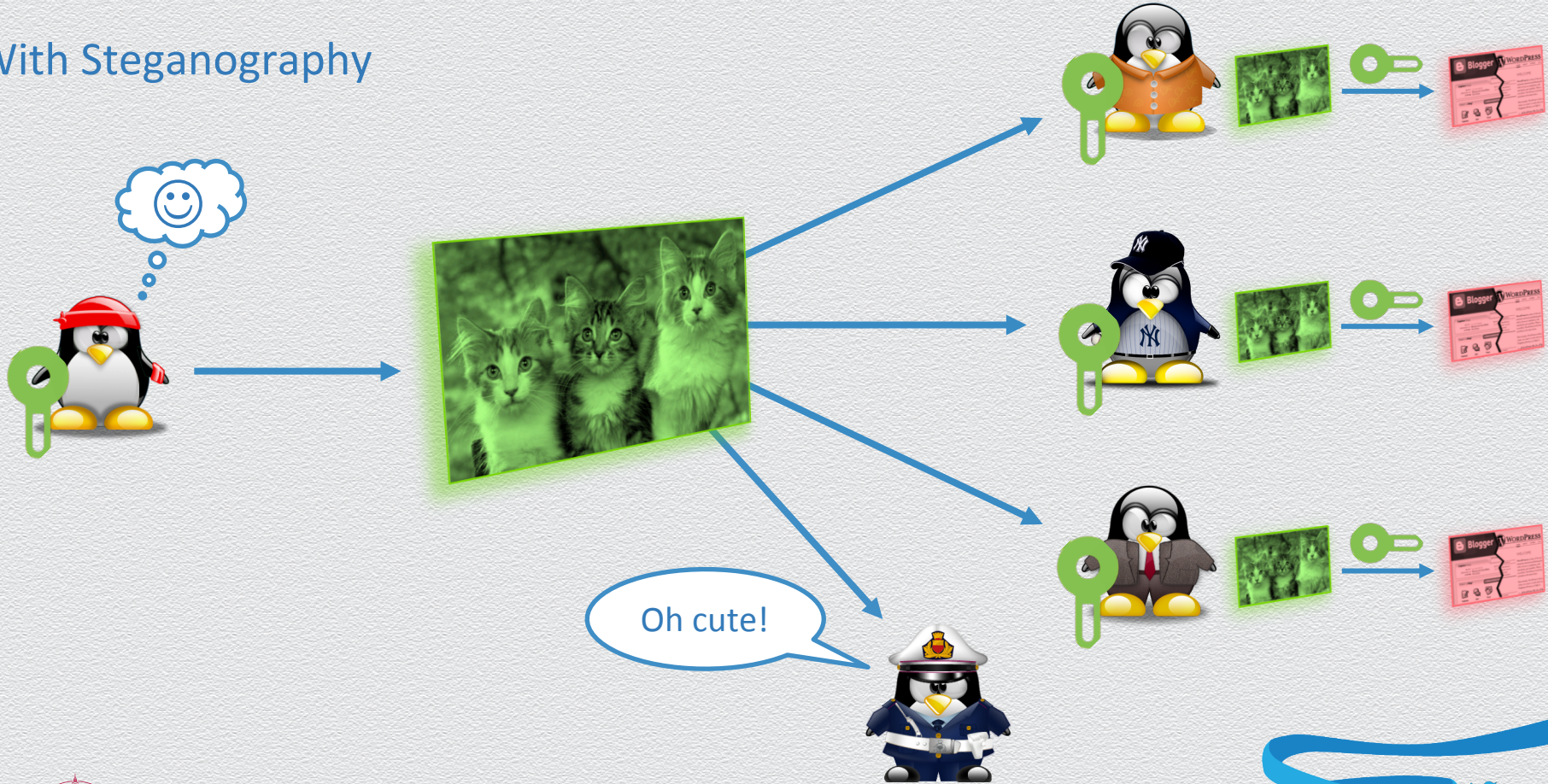


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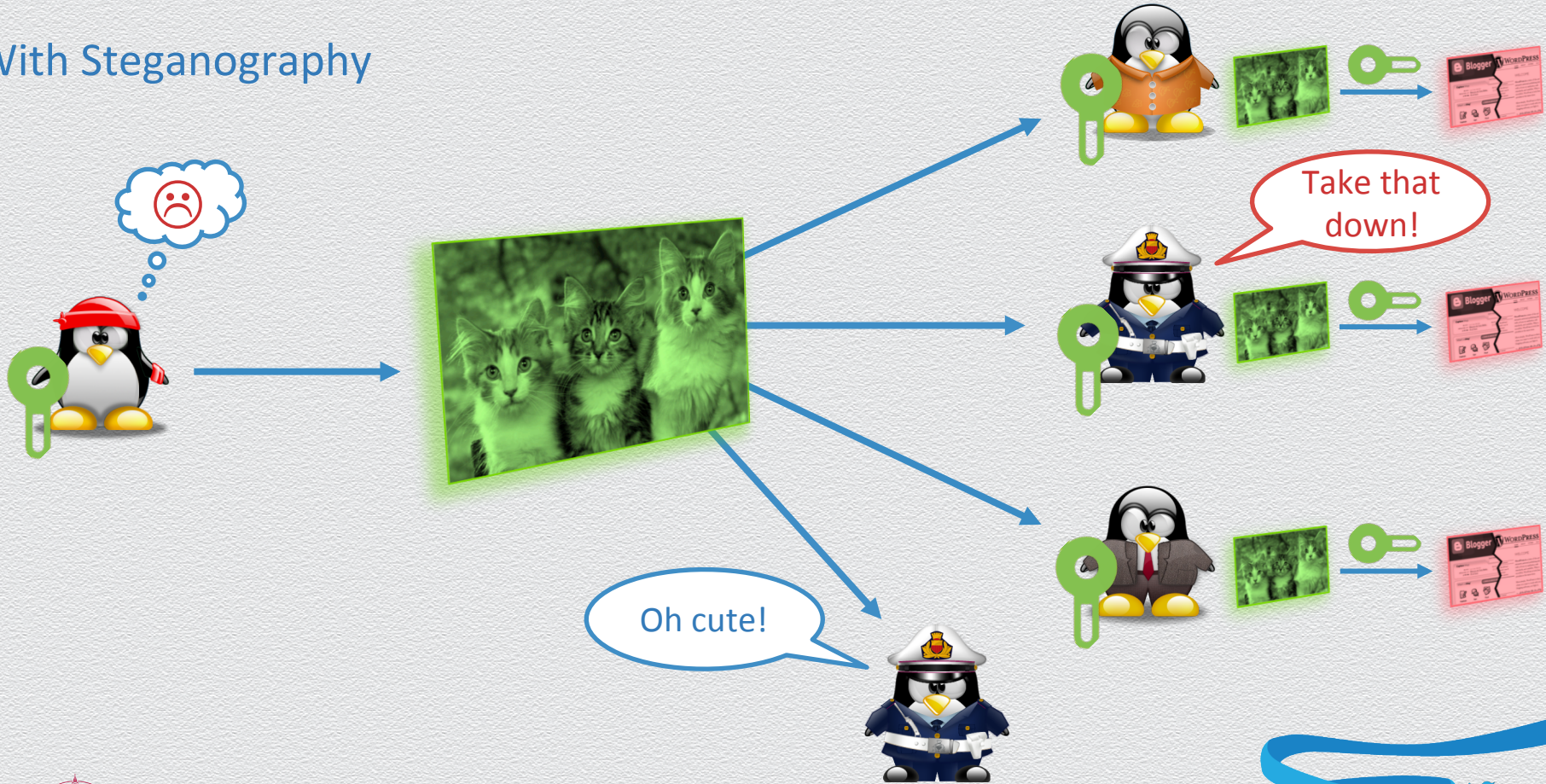


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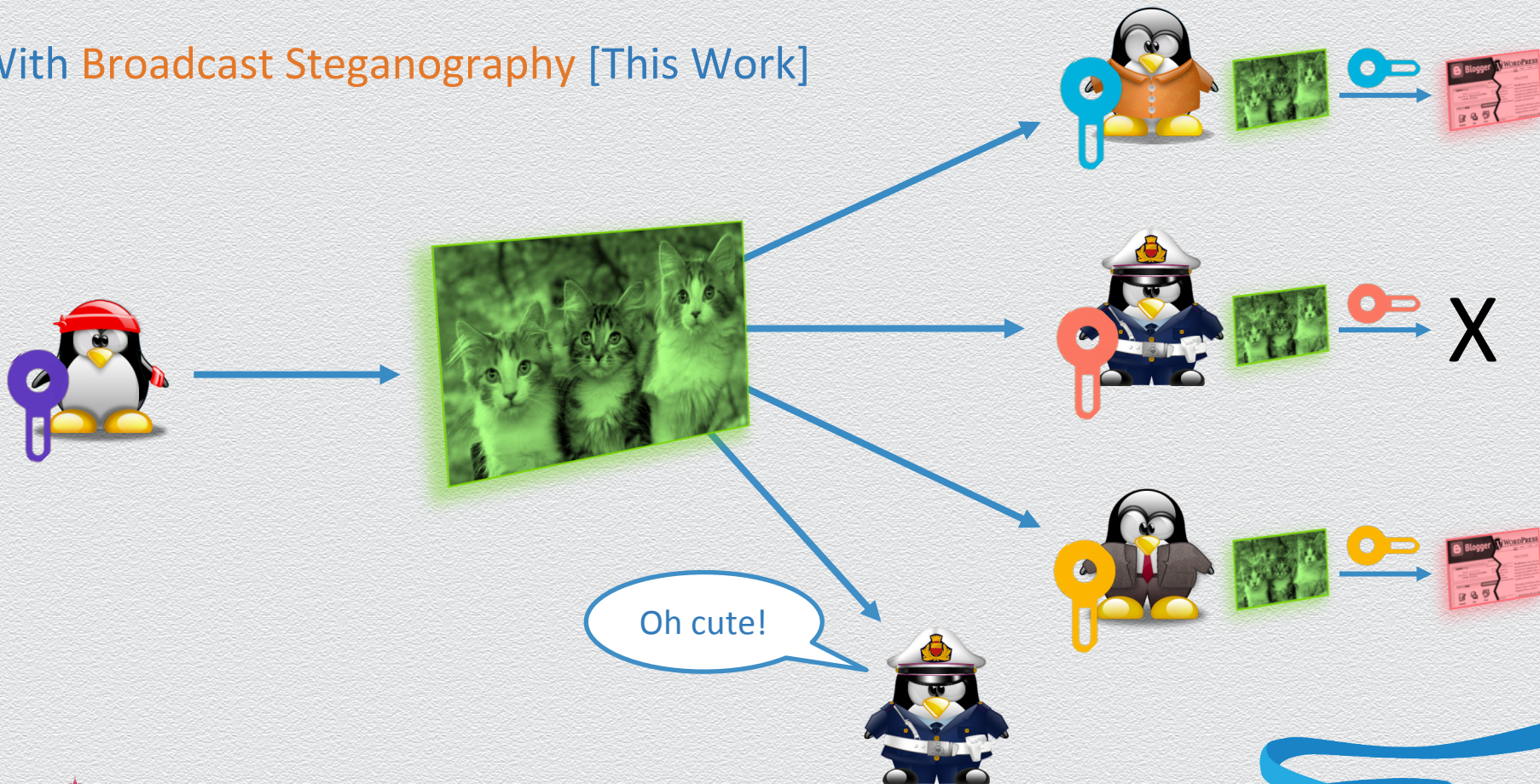


# With Broadcast Steganography [This Work]



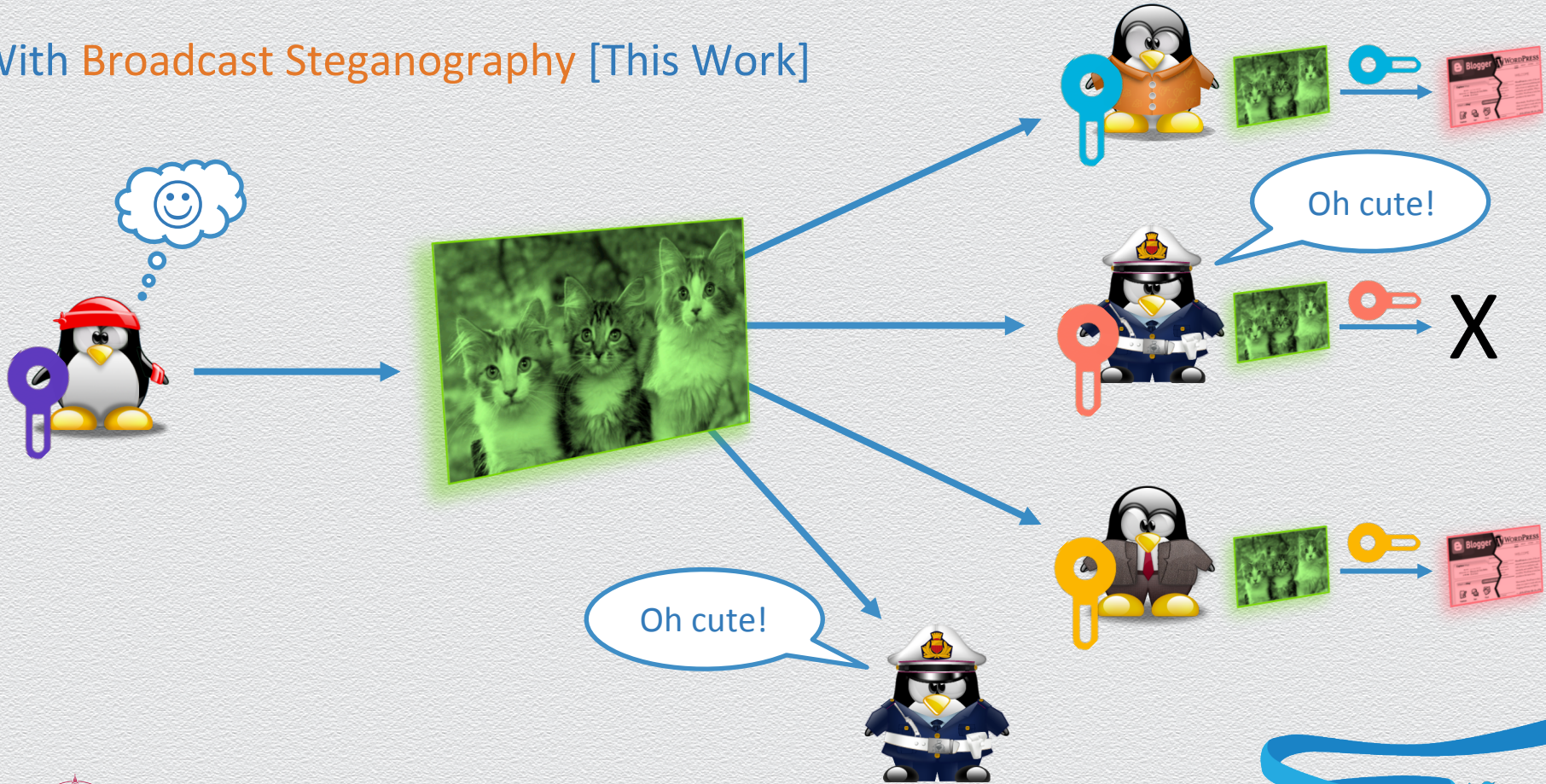


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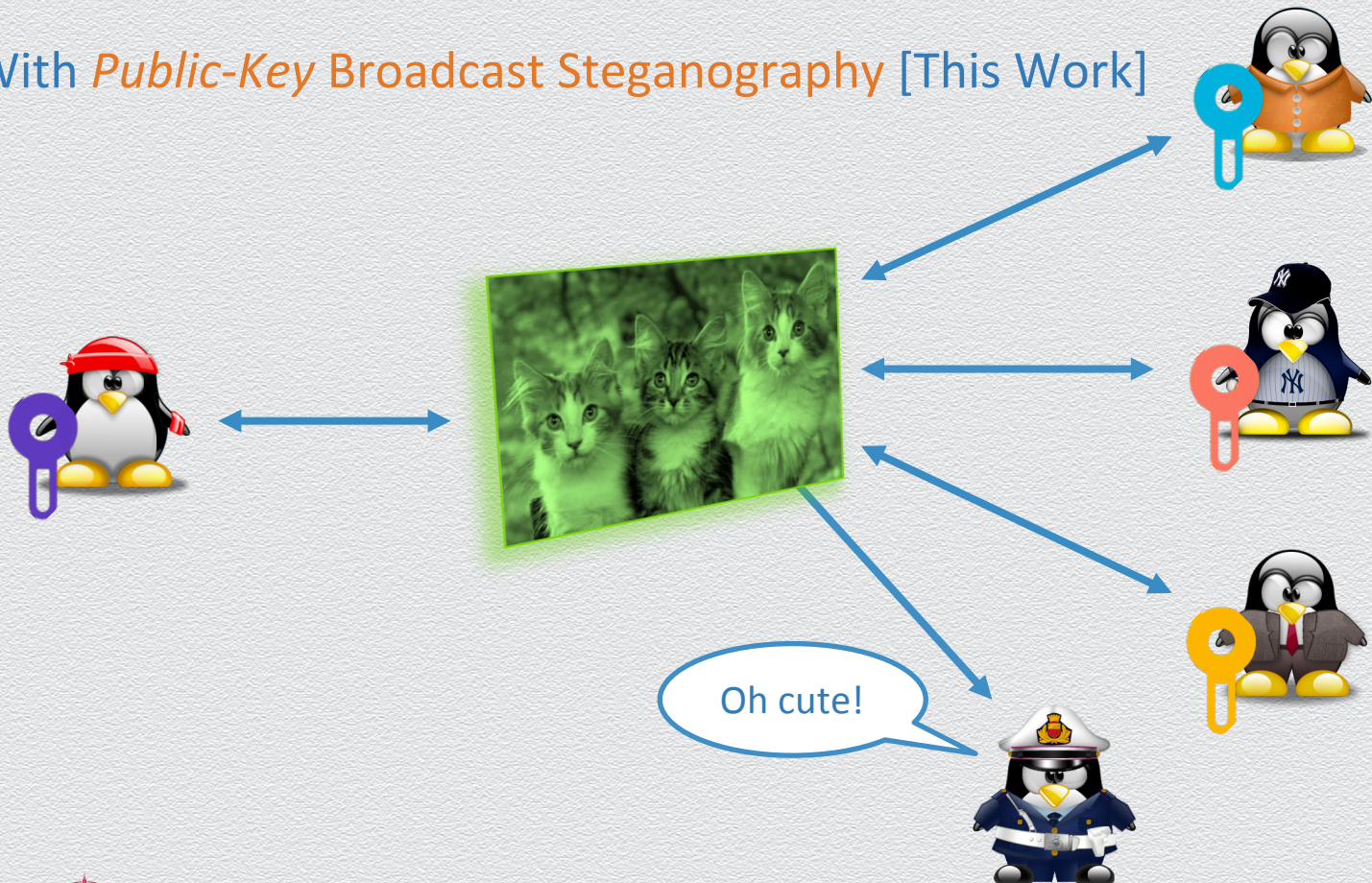


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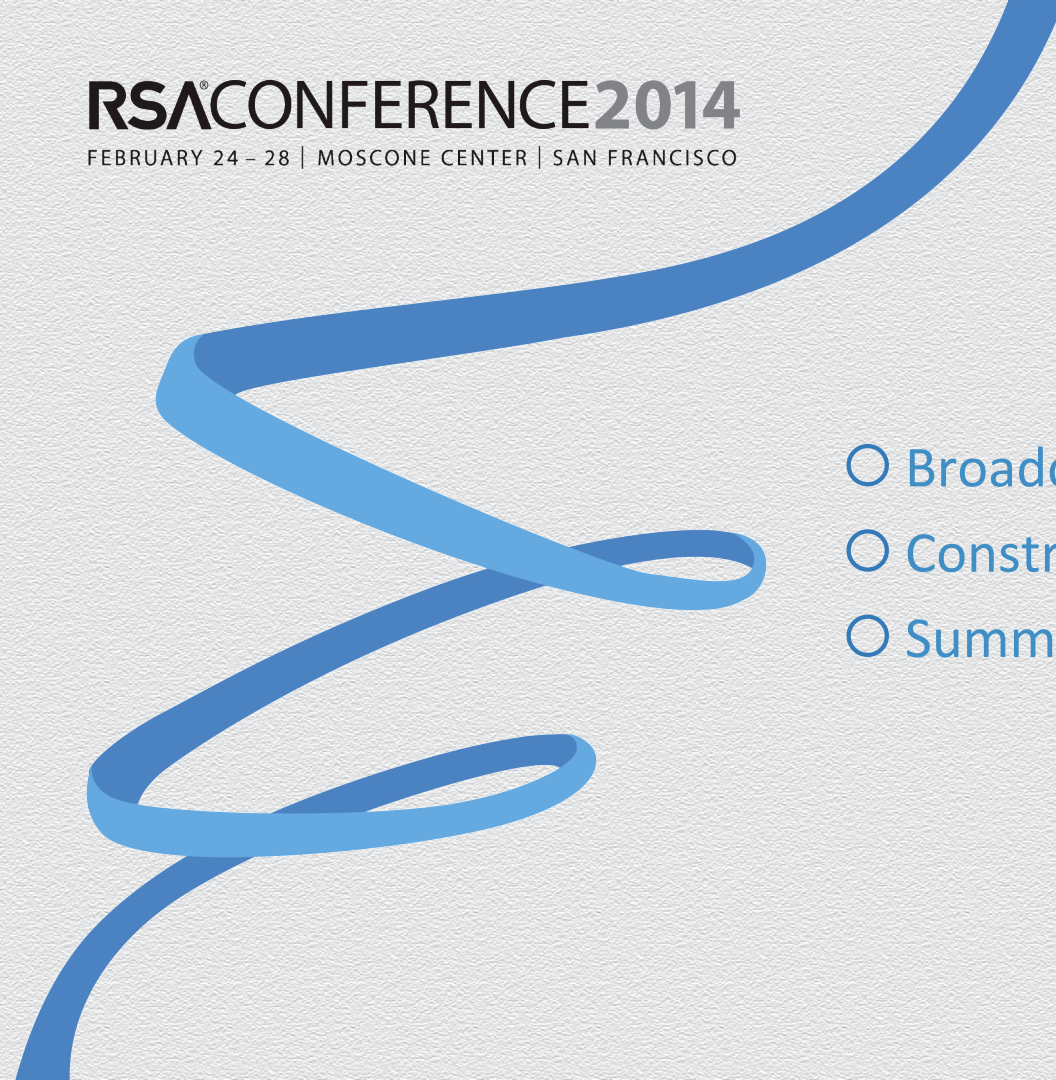
# With *Public-Key Broadcast Steganography* [This Work]





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- 
- Broadcast Steganography (BS)
  - Constructions
  - Summary



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# The Setting

Setup

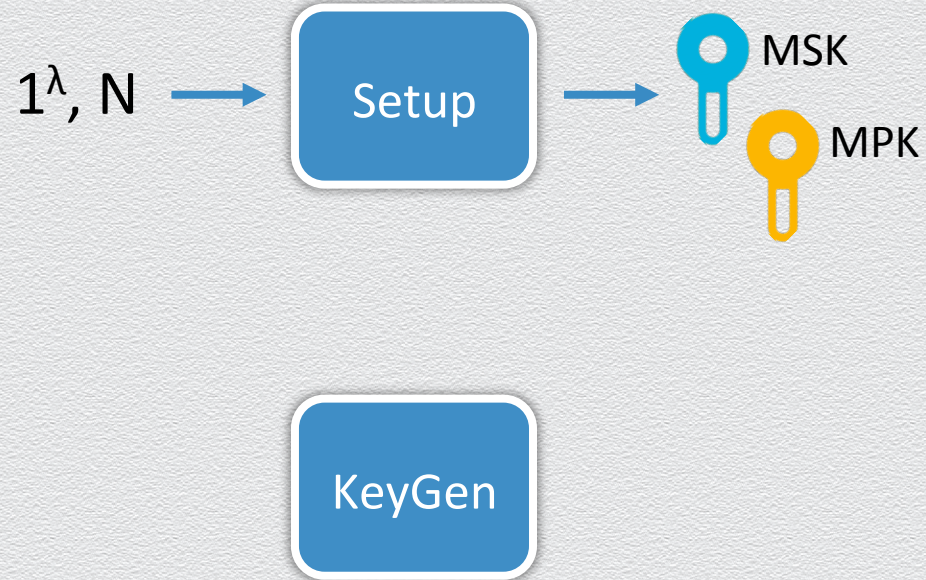


# The Setting



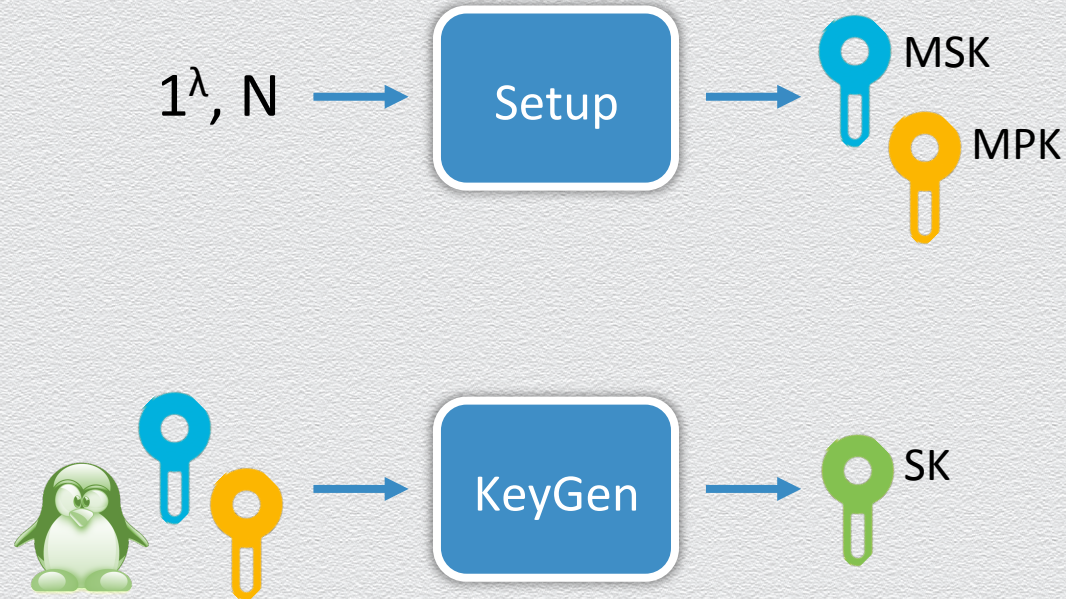


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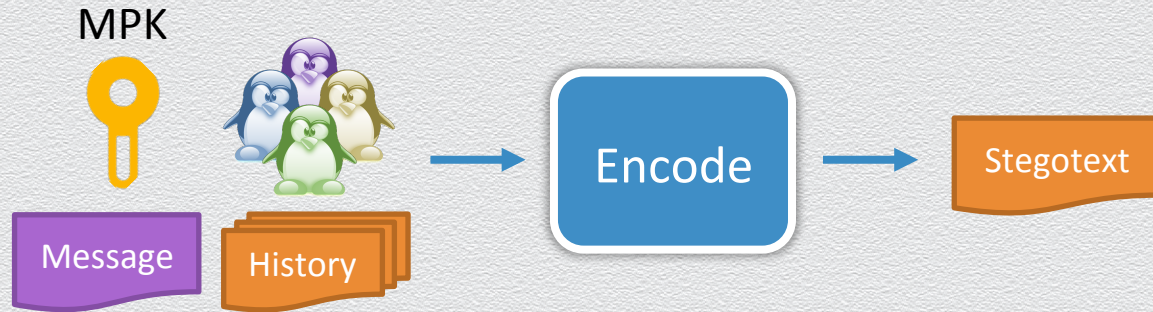


# The Setting

Encode

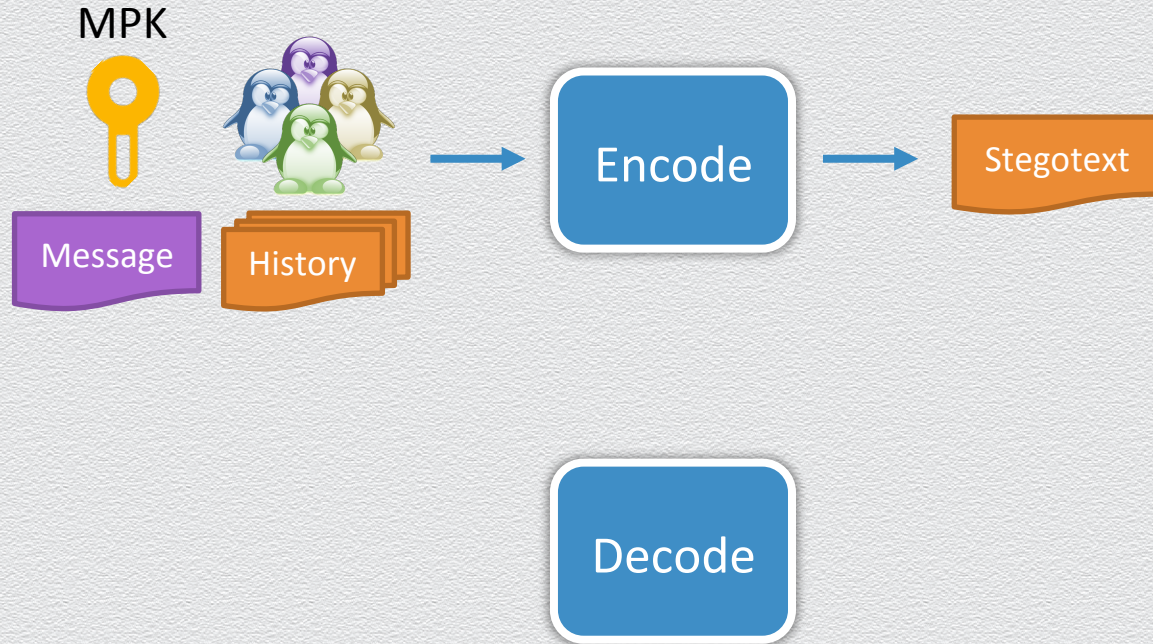


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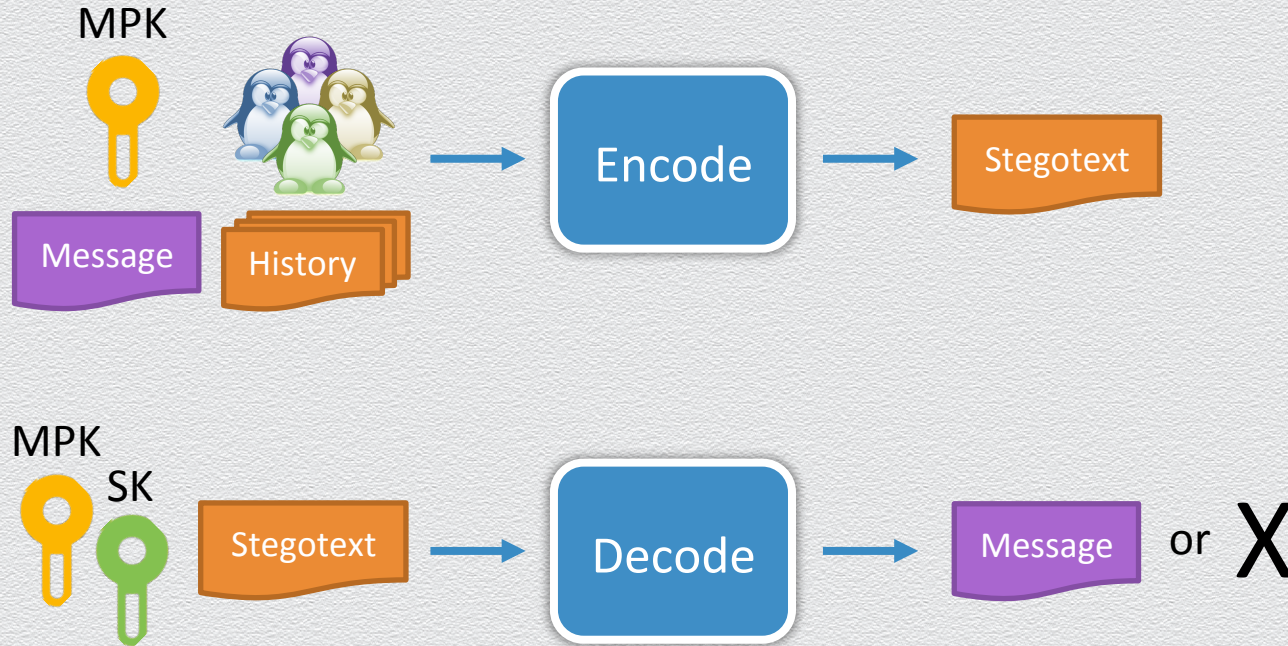


## The Setting





## The Setting





# The Security Model

1. Chosen-Coverttext Attack (BS-IND-CCA)
  - ◆ Analogous to BE-IND-CCA model
  - ◆ Adversary is allowed to corrupt users
  - ◆ Adversary is also given access to a decoding oracle
2. Publicly-Detectable Replayable Chosen Coverttext Attack (BS-IND-PDR-CCA)
  - ◆ Similar to BS-IND-CCA, but with **stricter** restrictions on allowable decoding queries
3. Chosen-Hiddentext Attack (BS-IND-CHA)
  - ◆ Analogous to BE-IND-CPA model
  - ◆ Adversary is only allowed to corrupt users
  - ◆ No decoding queries



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- ⦿ Broadcast Steganography (BS)

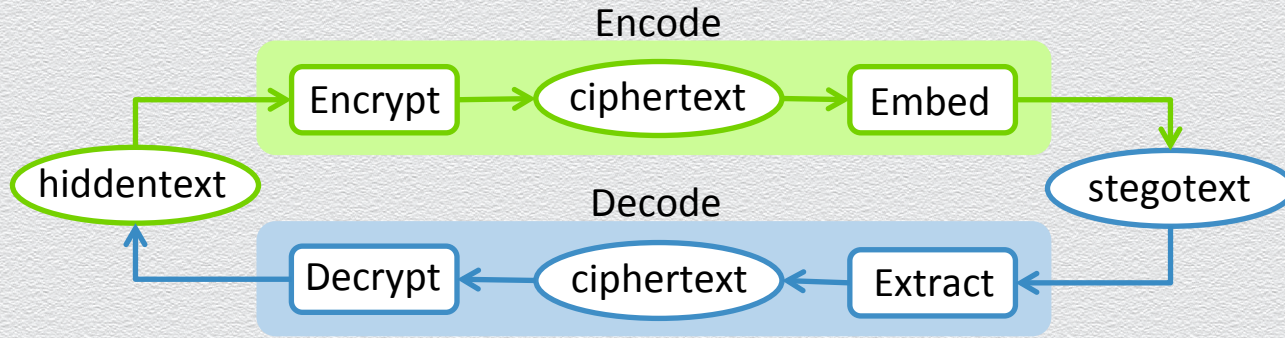
- ⦿ **Constructions**

- Summary



# Realizing Broadcast Steganography

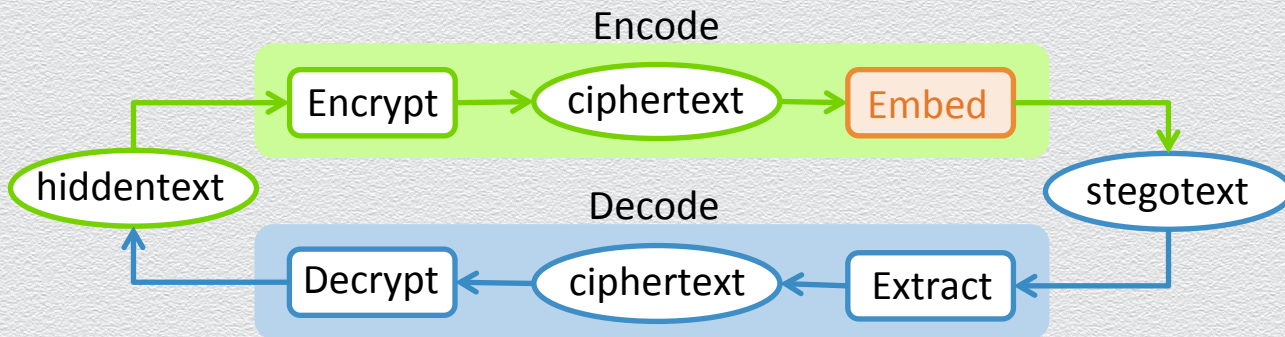
- ◆ Encrypt-then-Embed Paradigm [HLvA02, BaCa05]





# Realizing Broadcast Steganography

## ◆ Encrypt-then-Embed Paradigm [HLvA02, BaCa05]



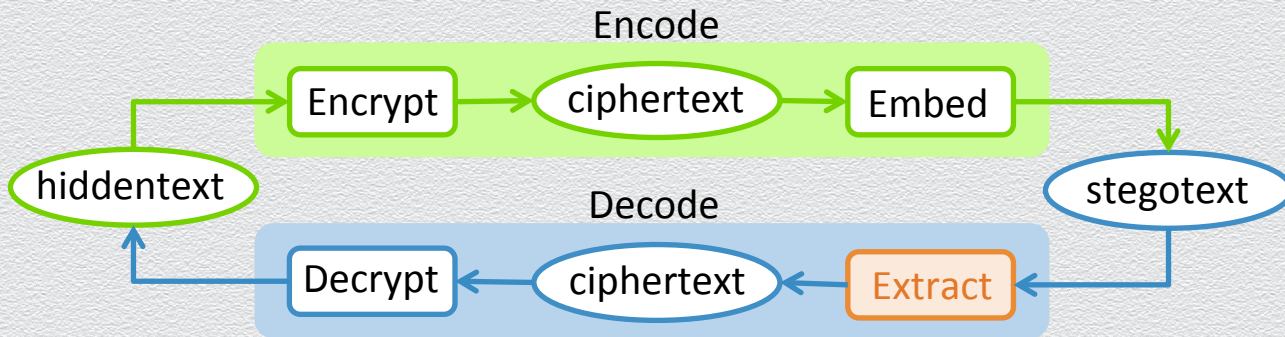
### ➤ Embed (rejection-sampling)

1. Let  $H$  be a strongly universal hash function
2. Break the ciphertext  $c$  into bits  $c_1, c_2, \dots, c_l$
3. To embed  $c_i$ , sample  $s_i$  from the channel until  $H(s_i) = c_i$
4. Output  $s = s_1 || s_2 || \dots || s_l$



# Realizing Broadcast Steganography

## ◆ Encrypt-then-Embed Paradigm [HLvA02, BaCa05]



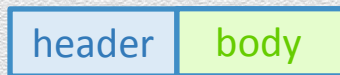
### ➤ Extract

1. Break the stegotext  $s$  into documents  $s_1, s_2, \dots, s_l$
2. Set  $c_i = H(s_i)$
3. Output  $c = c_1 || c_2 || \dots || c_l$



# Broadcast Encryption + Encrypt-then-Embed = Broadcast Steganography?

- ◆ Encrypt-then-Embed requires **pseudorandom** ciphertexts ...
- ◆ ... but, Broadcast ciphertexts have **structure**



broadcast ciphertext format

- ◆ Neither **header** nor **body** is pseudorandom



# Outsider-Anonymous Broadcast Encryption [FaPe12]

- ◆ Motivation: Anonymous Broadcast Encryption with short ciphertexts
  - ✧ A fully anonymous ciphertext length is subject to a linear lower bound [KiSa12]
  - ✧ In some applications, content may give recipient set away
    - ⇒ Suffices to protect anonymity of receivers from outsiders
- ◆ Outsider-Anonymity in Broadcast Encryption
  - ✧ Trades some degree of anonymity for better efficiency
  - ✧ Allows constructions with sub-linear ciphertext length



## oABE Encryption in [FaPe12]

### ◆ Encrypt( $S, m$ )

1. Group users in  $S$  into  $S'$ , a set of disjoint subsets
  - ✧  $|S'|$  is sub-linear in  $|S|$
2. Generate a ciphertext  $c_i$  for each  $s_i$  in  $S'$  (using anonymous IBE)
3. Attach a tag  $t_i$  to each  $c_i$  (for efficient decryption at the receivers)
4. Bundle all  $(t_i, c_i)$  components using one-time signature



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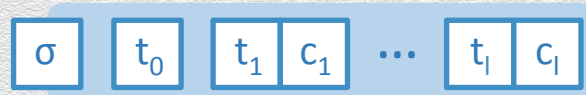




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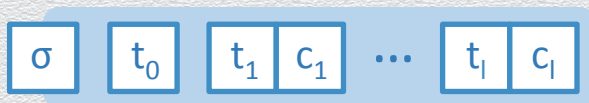




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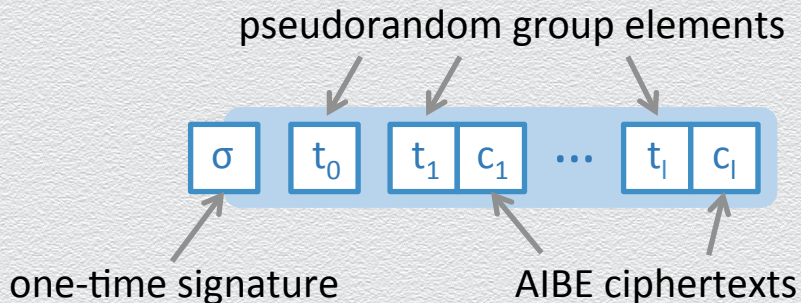
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- ◆ Notice that ciphertexts have **no header** ...
- ◆ ... but **still exhibit structure** due to tags and signature
- ◆ **Idea:** Toward a BS construction, make these components **pseudorandom**



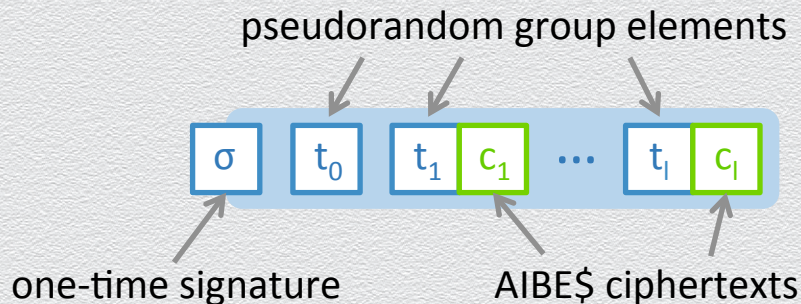
## oABE with Pseudorandom Ciphertexts (oABE\$) [This Work]



- ◆ How to make oABE ciphertexts **pseudorandom**?
  1. Replace the underlying AIBE with AIBE\$ [AgBo09]
  2. Apply an entropy smoothing hash to group elements
  3. Replace one-time signature with a MAC (implemented via PRF)



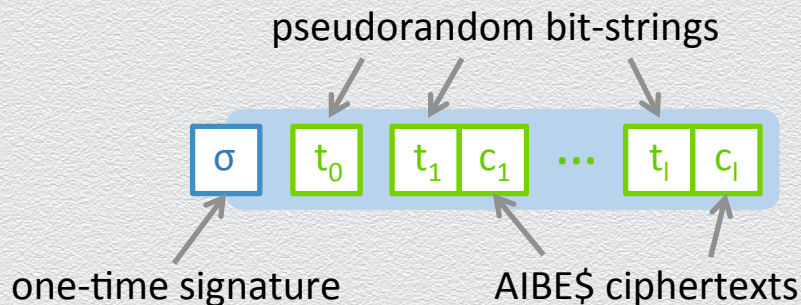
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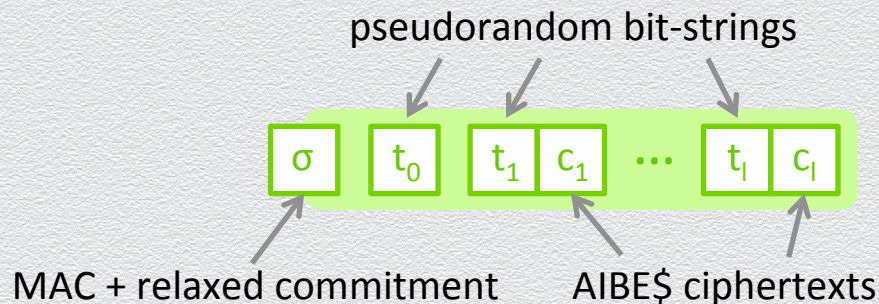
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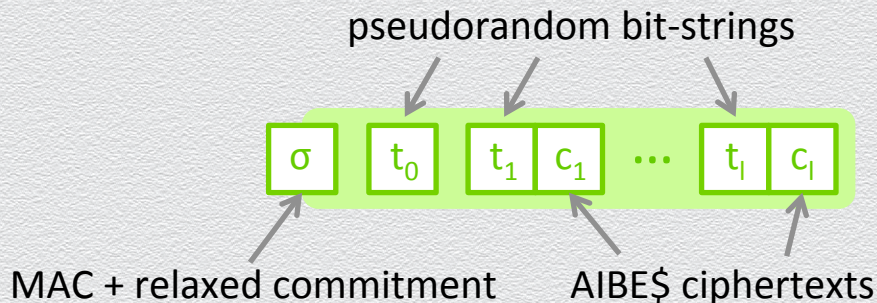
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**Question:** How to embed the MAC key in  $c_i$ 's and still obtain CCA security?

**Solution:** Construct an encapsulation mechanism [DoKa05, BoKa05]  
with **pseudorandom commitments**



## Comparison of BE Schemes with Anonymity Properties

Scheme	$ PK $	$ sk $	$ c $	Security Model	Anonymity
BBW06	$O(N)$	$O(1)$	$O(N-r)$	Static, RO	Full
LPQ12	$O(N)$	$O(1)$	$O(N-r)$	Adaptive, Standard	Full
FaPe12a	$O(N)$	$O(\log N)$	$O(r \log (N/r))$	Adaptive, Standard	Outsider
FaPe12b	$O(N \log N)$	$O(N)$	$O(r)$	Adaptive, Standard	Outsider
This Work	$O(N)$	$O(\log N)$	$O(r \log (N/r))$	Adaptive, Standard	Outsider

$N$ : total number of users,  $r$ : number of revoked users

- ◆ Only oABE\$ provides **pseudorandom** ciphertexts



# Our Construction of Broadcast Steganography

## ◆ Highlights

- ✧  $\text{oABE\$} + \text{Encrypt-then-Embed} = \text{Broadcast Steganography}$
- ✧ Our constructions have sub-linear stegotext length
- ✧ For CCA security, requires stateless channel

## ◆ Constructions:

1. BS-CHA
2. BS-PDR-CCA
3. BS-CCA



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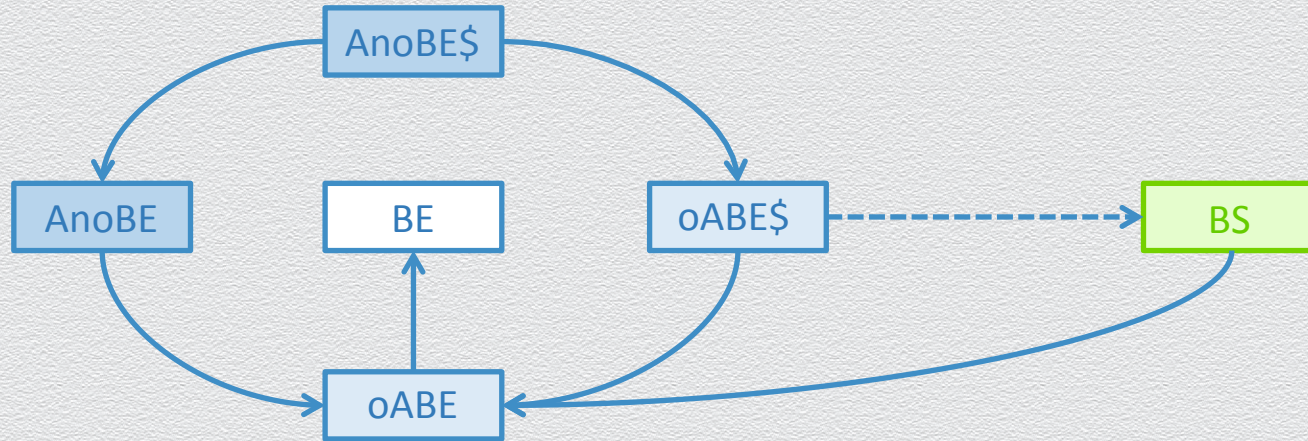
- ⦿ Broadcast Steganography (BS)

- ⦿ Constructions

- ⦿ Summary



## BE and Friends





# Summary

- ◆ Initiated the study of Broadcast Steganography
  - ✧ A multi-recipient communication tool to plant undetectable messages in innocent-looking conversations
- ◆ Put forth sublinear constructions of broadcast steganography under a range of security notions
- ◆ In the process, devised efficient broadcast encryption schemes with pseudorandom ciphertexts and anonymity properties
  - ✧ Implementing CCA checks without imposing structure on broadcast ciphertexts required overcoming multiple technical hurdles