Outsider-Anonymous Broadcast Encryption
with Sublinear Ciphertexts

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Motivation & State-of-the-Art

- **Crypto tools for secure multicast communications**
- **Broadcast Encryption (BE)**
  - Transmit data to a dynamically changing set of recipients
  - Info about receivers is broadcast in the clear

Receivers' identities are often sensitive.
Secure communication ought to protect more than just transmitted content!

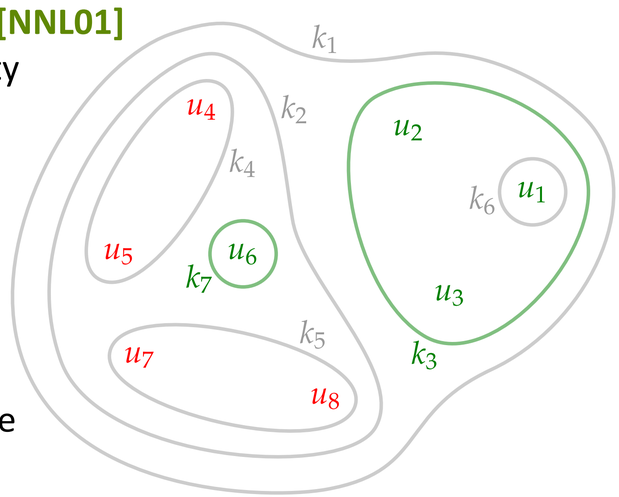
- **Anonymous BE (AnoBE):** also hides receiver set [BBW06]
  - Ciphertext linear in number of recipients
  - Security model against static adversary
  - Security of enhanced construction based on the ROM
  - [LPQ12] recently removed ROM + active adversary

Applications

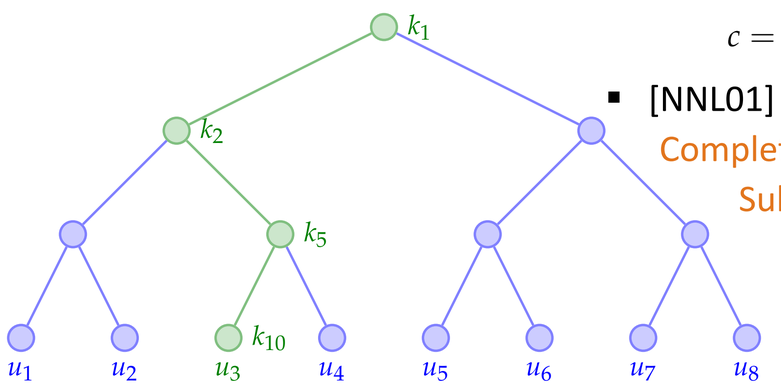
- **Networking technology for military operations**
  - AnoBE enables secure distribution of tactical data in missions with ad-hoc team formation while concealing identities of operatives authorized to access content
- **BE enables efficient encrypted file systems**
  - AnoBE avoids disclosure of identities of authorized users, not only from outsiders, but also from one another

Primitives

- **Anonymous Identity-based Encryption (AIBE)**
  - A public-key encryption scheme where the user public key is an arbitrary bit-string
  - Ciphertext hides the identity under which it is encrypted
- **The Subset Cover (SC) Framework [NNL01]**
  - **Goal:** Define and analyze security of revocation schemes in the private-key setting
  - Users belong to multiple subsets with associated keys
  - To broadcast a message, first find the cover set, and then hybrid-encrypt the message under the keys of the coverset



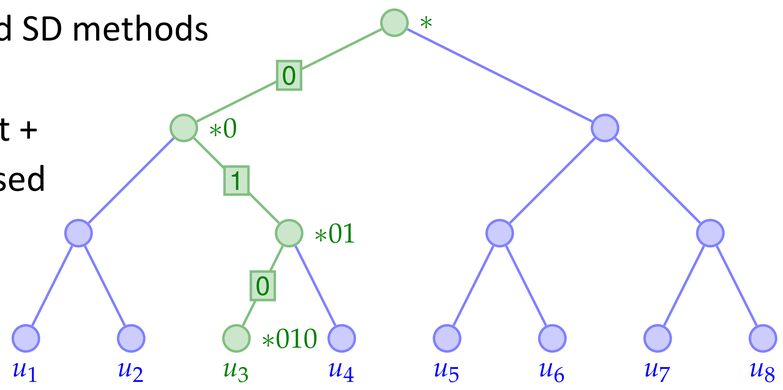
$c = (E_s(m), E_{k_7}(s), E_{k_3}(s))$



- [NNL01] presents two SC algorithms: Complete Subtree (CS) method and Subset Difference (SD) method

Private-Key Complete Subtree Method of [NNL01]

- **Extension of the Subset Cover Framework to Public-Key Setting [DF02]**
  - [DF02] extends the CS and SD methods to the public-key setting
  - **Idea:** Novel ID assignment + (Hierarchical) Identity-Based Encryption ((H)IBE)



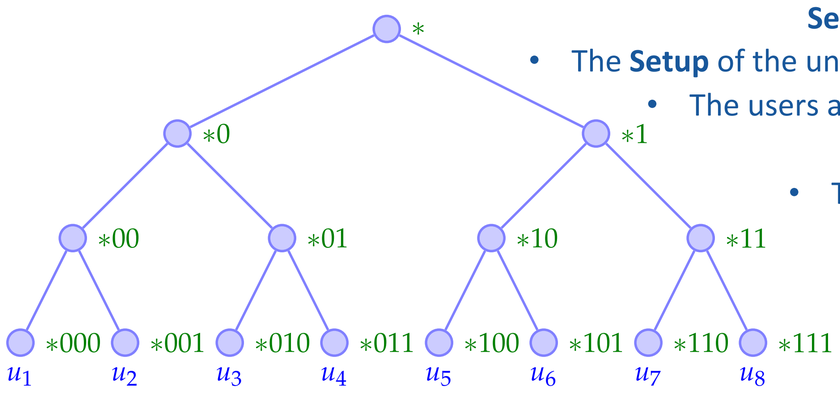
Public-Key Complete Subtree Method of [DF02]

Our Contribution (Published at PKC'12)

- **Outsider-Anonymous Broadcast Encryption (oABE)**
  - Relaxing receiver anonymity guarantees for better efficiency
  - Recipient's identities hidden from outsiders…
  - … but individual recipients might learn about each other
  - Attain sub-linear ciphertexts in the number of recipients (in the standard model), and security against active adversary

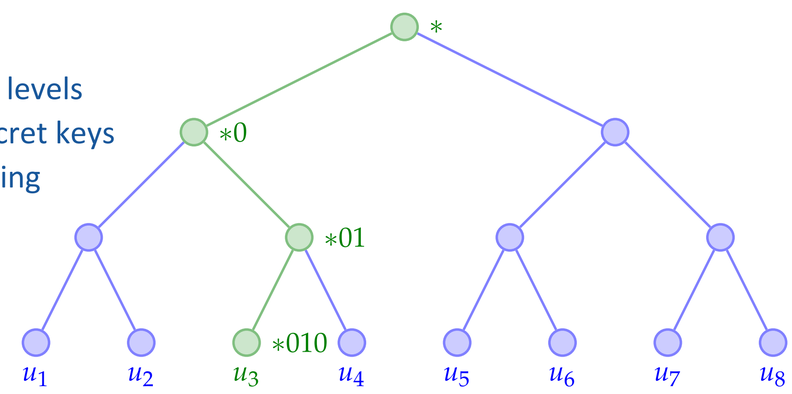
Our Constructions

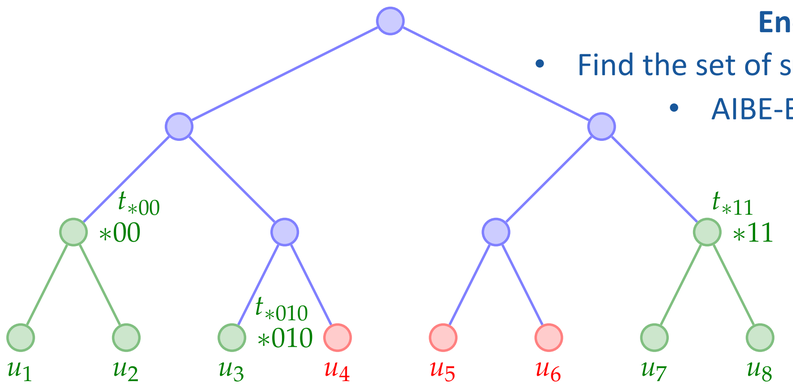
- **Idea:** PK-CS method + Anonymous IBE = oABE
- Generic CPA, Generic CCA, CCA with enhanced decryption



Setup
- The **Setup** of the underlying AIBE scheme is run
- The users are denoted by the leaves of a perfect binary tree
- The subtrees of this tree are the possible subsets

KeyGen
- Each u_i belongs to $log(N)+1$ levels
- u_i is given $log(N)+1$ AIBE secret keys of the identities corresponding to the ancestor nodes in those levels





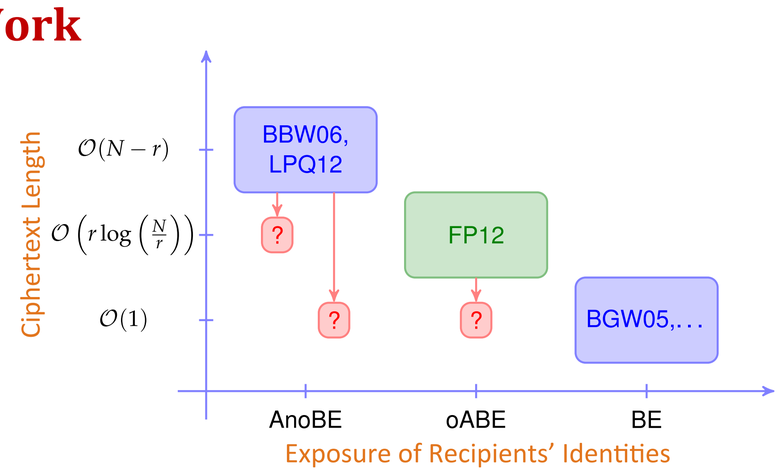
Encrypt/Decrypt
- Find the set of subtrees covering the recipients
- AIBE-Encrypt the message under the identities corresponding to the root nodes of those subtrees
- Also attach a "tag" to each ciphertext to allow efficient decryption at the receivers

Comparisons

	Scheme	PK Length	SK Length	CT Length	Decryption Attempts
Regular	BBW06	$\mathcal{O}(N)$	$\mathcal{O}(1)$	$\mathcal{O}(N-r)$	$\mathcal{O}(N-r)$
	LPQ12	$\mathcal{O}(N)$	$\mathcal{O}(1)$	$\mathcal{O}(N-r)$	$\mathcal{O}(N-r)$
	FP12a	$\mathcal{O}(1)$	$\mathcal{O}(\log N)$	$\mathcal{O}\left(r\log\left(\frac{N}{r}\right)\right)$	$\mathcal{O}\left(r\log\left(\frac{N}{r}\right)\log N\right)$
Enhanced	BBW06	$\mathcal{O}(N)$	$\mathcal{O}(1)$	$\mathcal{O}(N-r)$	1
	LPQ12	$\mathcal{O}(N)$	$\mathcal{O}(1)$	$\mathcal{O}(N-r)$	1
	FP12a	$\mathcal{O}(N)$	$\mathcal{O}(\log N)$	$\mathcal{O}\left(r\log\left(\frac{N}{r}\right)\right)$	1
	FP12b	$\mathcal{O}(N^2)$	$\mathcal{O}(N)$	$\mathcal{O}(r)$	1

N: total number of users. r: number of revoked users.

Future Work



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